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**KIRIRI WOMENS' UNIVERSITY OF SCIENCE AND TECHNOLOGY**  
**UNIVERSITY EXAMINATION, 2016/2017 ACADEMIC YEAR**  
**FIRST YEAR, FIRST SEMESTER EXAMINATION**  
**FOR THE DEGREE OF BACHELOR OF SCIENCE**  
**(MATHEMATICS)**

Date: 11<sup>th</sup> August, 2016.  
Time: 8.30am – 10.30am

**KMA 104 - CALCULUS I**

**INSTRUCTIONS TO CANDIDATES**

**ANSWER QUESTION ONE (COMPULSORY) AND ANY OTHER TWO QUESTIONS**

**QUESTION ONE (30 MARKS)**

- a) i) Define a function and give two relations; one that is a function and one that is not a function. (2 Marks)
- ii) Determine the range of;  $f(x) = \frac{2x}{x^2-4}$  and  $f(x) = 2^x$  (2 Marks)
- b) Evaluate the following limit; (3 Marks)
- $$\lim_{x \rightarrow 3} \frac{x-3}{x^2-9}$$
- c) Determine the slope of the following functions; (3 Marks)
- i)  $f(x) = (4x^2 - 2)^3(3x - 2x^3)^5$  (3 Marks)
- ii)  $f(x) = \left(\frac{4x^2+x}{1+2x^2}\right)^5$  (4 Marks)
- iii)  $g(x) = \tan(x^2 - 4x) \cos(x^2 - 4x) + \sec(x^2 - 4x)$  (4 Marks)
- d) Given that  $2xy^3 + x^2 = \sin(x + y)$  find; (4 Marks)
- i)  $\frac{dy}{dx}$  (4 Marks)
- ii)  $\frac{d^2y}{dx^2}$  at  $\left(\frac{\pi}{2}, \frac{\pi}{4}\right)$ . (4 Marks)

- e) Find the area between  $y = 4x + 6$  and  $y = 2x^2 - 4x + 12$  (4 Marks)

**QUESTION TWO (20 MARKS)**

- a) Find the derivative of the following function;

$$f(x) = \frac{3x^2 + 5}{x^3 - 10}$$

(4 Marks)

- b) For what values of  $x$  does  $y = (x - 5)^3(x - 1)^2$  have a horizontal tangent. (5 Marks)

- c) Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$  given that;  $y = \frac{\ln x - 4x}{x^2}$  (6 Marks)

- d) A body initially at rest is projected in a straight line. If its displacement is  $s(t) = 12t - 5t^2$
- i) Find the velocity of the body after 2 seconds. (2 Marks)
- ii) The total time taken for the body to come down. (3 Marks)

**QUESTION THREE (20 MARKS)**

- a) Evaluate the following;  $\int_0^1 2x(x^2 - 1)^3 dx$  (4 Marks)

- b) Differentiate the following;

i)  $f(x) = \frac{1}{(3-12x-4x^2)e^{3x-x^2}}$  (4 Marks)

ii)  $\sec(x + 1)^2 \tan(x - 1)^2$  (5 Marks)

- c) Evaluate the limit;

$$\lim_{x \rightarrow 0} \frac{4x^2 - 2 \sin 2x}{x}$$

(4 Marks)

- d) Determine if  $f(x) = \frac{x^2 - 1}{x + 1}$  is continuous at  $x = -1$ . (3 Marks)

**QUESTION FOUR (20 MARKS)**

- a) State the Rolle's Theorem. (3 Marks)
- b) Verify Rolle's Theorem for  $f(t) = 2t - t^2 - t^3$  on  $[-2, 1]$ . (6 Marks)

c) Differentiate;  $\frac{5}{2x-3}$   
From the first principal. (5 Marks)

d) Find the inverse of the function;

$$f(x) = \frac{2x - 5}{x + 3}$$

(3 Marks)

e) Use chain rule to determine the derivative of  $y = 8 \cot(4x - \pi)$

(3 Marks)

**QUESTION FIVE (20 MARKS)**

a) Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$  given that;

$$x(r) = r^2 - r \text{ and } y(r) = \frac{2}{3}r^3 + \frac{1}{2}r^2 - r.$$

(6 Marks)

b) Find the slope of;  $2x + 2y = (x + y + 1)^2$  at  $(1,0)$ .

(4 Marks)

c) Discuss the continuity of;  $f(x) = \begin{cases} 4x + 1 & \text{for } x \leq 0 \\ 1 - 2x & \text{for } x > 0 \end{cases}$  at  $x = 0$ .

(5 Marks)

d) Find  $f'(0)$  and  $f'\left(\frac{\pi}{8}\right)$  given that  $f(x) = \cos 2x + \sec 2x$

(5 Marks)