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KIRIRI WOMENS' UNIVERSITY OF SCIENCE AND TECHNOLOGY
UNIVERSITY EXAMINATION, 2023/2024 ACADEMIC YEAR
FIRST YEAR, FIRST SEMESTER EXAMINATION
FOR THE DEGREE OF BACHELOR OF SCIENCE
(MATHEMATICS
Date: $6^{\text {th }}$ December, 2023
Time: 8.30am - 10.30am

## KMA 100 - FOUNDATION MATHEMATICS

## INSTRUCTIONS TO CANDIDATES

ANSWER QUESTION ONE (COMPULSORY) AND ANY OTHER TWO QUESTIONS

## QUESTION ONE (30 MARKS)

a) Solve for $x$ if $\left(\frac{2}{3}\right)^{x}=\frac{1}{16}$.
(3 marks)
b) Prove that, if the sum of the squares of the roots of the equation $a x^{2}+b x+c=0$ is 1 , then $b^{2}=2 a c+a^{2}$.
(3 marks)
c) A polynomial $f(x)$ has remainder 9 when divided by $(x-3)$ and remainder -5 when divided by $(2 x+1)$. Find the remainder when divided by $(x-3)(2 x+1)$.
d) Solve the equation $2 \log _{5} x+2 \log _{x} 5=5$
e) $\quad$ Simplify $\frac{\sqrt{x y} \times x^{\frac{1}{1}} \times 2 y^{\frac{1}{4}}}{\left(x^{10} y^{9}\right)^{\frac{1}{12}}}$
f) Find without table or calculators the value of $-\operatorname{Sin} 45 \operatorname{Sin} 57+3 \operatorname{Cos} 33 \operatorname{Cos} 60$
g) The eighth and fifth terms of a G.P are 4374 and 162 respectively. Determine the seventh term.
h) Solve the following quadratic equation;
i) $x^{2}+15 x+54=0$ by factorization method
ii) $\quad x^{2}-5 x-1=0$ by completing squares method

## QUESTION TWO (20 MARKS)

a) Rationalize the denominator in $\frac{3}{\sqrt[5]{2}}$
(2 marks)
b) Expand $(1-3 x)^{8}$ up to the term in $x^{5}$ hence use your expansion to estimate $(0.998)^{8}$ correct to five decimal places.
c) Factorize completely the expression $x^{4}+5 x^{3}+5 x^{2}-5 x-6$ hence solve the equation $x^{4}+5 x^{3}+5 x^{2}-5 x-6=0$
(4 marks)
d) The roots of the equation $2 x^{2}-4 x+1=0$ are $\alpha$ and $\beta$. Find an equation with integral coefficient whose roots are $2-\alpha$ and $2-\beta$
e) $\quad$ Show that $\log _{3^{n}} x=\frac{1}{n} \log _{3} x$.

Hence solve the equation $\log _{81} x+\log _{3} x+\log _{\sqrt{3}} x=13$
f) Determine the number of permutations of the letters of the word POPULATION.
(3 marks)

## QUESTION THREE (20 MARKS)

a) How many even numbers greater than 50000 can be formed using the digits $0,3,4,5,6,7$
i) without repetitions
(6 marks)
ii) if repetitions are allowed
(4 marks)
b) Find the first four terms in the expansion of $(1-8 x)^{\frac{1}{2}}$ in ascending powers of $x$. Hence, substitute $x=\frac{1}{100}$ and obtain the value of $\sqrt{23}$ correct to 5 significant figures.
(6 marks)
c) State the quotient and the remainder when $6 x^{3}-8 x+5$ is divided by $2 x-4$.
(4 marks)

## QUESTION FOUR (20 MARKS)

a) Find $y$ in terms of $x$ if $\log \left(\frac{x^{2}}{y}\right)=5-2 \log x$
b) A customer makes deposits of Ksh.10,000 on first January every year for four years. How much is the investment worth at the end of the four years if it attracts a compound interest of $12 \%$ per annum?
(6 marks)
c) Show that $\tan (A+B)=\frac{\tan A+\tan B}{1-\tan A \tan B}$
(6 marks)
d) Find the value of $\log _{3} \frac{1}{27}$
(4 marks)

## QUESTION FIVE( 20 MARKS)

a) The second and fifth terms of an arithmetic series are 26 and 41 respectively.
i) Show that the common difference of the series is 5
(4 marks)
ii) Find the $12^{\text {th }}$ term of the series
(3 marks)
iii) Another arithmetic series has first term -12 and common difference 7. Given that the sums of the first $n$ terms of these two series are equal, find the value of $n$.
b) Use the Pascal's triangle to expand $(2 x-3)^{7}$
c) A committee of six is to be formed from nine women and three men. In how many ways can the members be chosen so as to include at least one man?

